

Immediate (deductive) inference

$A \not\vdash \bar{\top}$ For example, All snakes are poisonous implies some snakes are poisonous (assuming the subject satisfies the condition of existential import—at least one instance of the subject exists)

$A \vdash \sim(O)$

$A \vdash \sim(E)$

$E \vdash O$

$I \vdash \sim(E)$

$\sim(A) \vdash O$

$\sim(E) \vdash I$

$\sim(I) \vdash E$

$\sim(I) \vdash O$

$\sim(O) \vdash A$

$\sim(O) \vdash I$

$E \vdash \sim(A)$

$E \vdash \sim(I)$

$\sim(I) \vdash \sim(A)$

$O \vdash \sim(A)$

$\sim(O) \vdash \sim(E)$

\dashv means “does not imply or entail, or cannot be deduced from”. I.e., Given that it is not the case that All S is P, one cannot deduce that No S is P. The fact that “it is not the case that All men are Italian” does not permit us to conclude that No men are Italian.

$\sim(A) \dashv E$ (E is not deducible from $\sim(A)$, but remains unknown).

$\sim(A) \dashv I$ (If we know it is false that all men are geniuses, we do not thereby know that some men are geniuses)

$\sim(E) \dashv A$ (If we know that it is false that no men are geniuses, we do not thereby know that all men are geniuses)

$\sim(E) \dashv O$ (and we do not thereby know that some men are not geniuses; they could all be geniuses for all we know).

$I \dashv A$ (knowing that some men are geniuses does not tell us whether or not all men are geniuses)

$I \dashv O$ (knowing that some men are geniuses does not tell us whether some men are not geniuses)

$O \dashv E$ (knowing that some men are not geniuses does not tell us whether no man is a genius)

$O \dashv I$ (knowing that some men are not geniuses does not tell us that some men are geniuses)